

Bonus Problem

Remark: This problem is harder than homework or recommended problems.

Let G be the unit-distance graph in the plane: $V(G) = \mathbb{R}^2$, and two points are adjacent iff their Euclidean distance is 1 (this is an infinite graph). Prove that $4 \leq \chi(G) \leq 7$.