

## 9th lesson

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### Theory

### Exercises

1. Find and sketch the contourlines = levelsets:

(a)  $f(x, y) = 2x + 3y + 1$

(e)  $f(x, y) = y^2 - x^2$

(b)  $f(x, y) = x^2 + y^2$

(f)  $f(x, y) = x^2 - y$

(c)  $f(x, y) = \sqrt{x^2 + y^2}$

(g)  $f(x, y) = e^y - x^2$  (use a program)

(d)  $f(x, y) = \sqrt{64 - x^2 - y^2}$

2. Find and sketch the levelsurfaces:

(a)  $f(x, y, z) = x^2 + y^2 + z^2$

(c)  $f(x, y, z) = x^2 + y^2$

(b)  $f(x, y, z) = 4x^2 + y^2 + z^2$

(d)  $f(x, y, z) = z - y$

3. Describe the shape of the cross-sections:

(a)  $f(x, y) = x^2 + y^2$

(e)  $f(x, y) = e^{-(x^2+y^2)} \sin(x^2 + y^2)$   
(use a program)

(b)  $f(x, y) = x^2 - y^2$

(c)  $f(x, y) = (x - y)^2$

(d)  $f(x, y) = |x| + |y|$

(f)  $f(x, y) = \sin(x - y)$