

# ∫ Antiderivative

$$\begin{array}{ccc} f & & x^2 \\ \boxed{\downarrow} \text{ Der} & & \downarrow \\ f' & & 2x \end{array}$$

$$\int 2x \, dx \stackrel{c}{=} x^2 \quad \int \sin x \, dx \stackrel{c}{=} -\cos x$$

$$\int e^x \, dx = e^x + c \quad \int \cos x \, dx \stackrel{c}{=} \sin x$$

$$\int \frac{1}{1+x^2} \, dx \stackrel{c}{=} \arctan x$$

$$\int 2x \, dx = \underline{x^2 + c} \quad \underline{x \in \mathbb{R}}$$

$$\int \frac{1}{\sqrt{1-x^2}} \, dx = \arcsin x$$

$$\downarrow \\ \underline{x \in (-1, 1)}$$

$$\downarrow \\ \underline{x \in [-1, 1]}$$

$$\begin{array}{l} 1 - x^2 > 0 \\ 1 > x^2 \end{array}$$



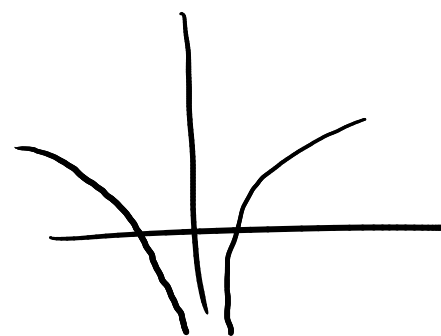
$$\int \frac{1}{x} \, dx = \underline{\ln |x| + c}$$

$$x \in (-\infty, 0)$$

$$x \in (0, \infty)$$

$$n \neq -1$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1}$$



$$\int x^3 \, dx \stackrel{c}{=} \frac{x^{3+1}}{3+1} = \frac{x^4}{4}$$

$$\int \sqrt{x} \, dx = \int x^{1/2} \, dx \stackrel{c}{=} \frac{x^{1/2+1}}{1/2+1} = \frac{x^{3/2}}{3/2} = \frac{2}{3} \sqrt{x^3}$$

$$x \in \underline{[0, \infty)}$$

$$\int \frac{1}{x^2} dx = \int x^{-2} dx \stackrel{C}{=} \frac{x^{-2+1}}{-2+1} = \frac{x^{-1}}{-1} = -\frac{1}{x}$$

$x \in (-\infty, 0) \cup (0, \infty)$

$$\int 2e^x - \frac{1}{3} \frac{1}{\cos^3 x} dx = 2e^x - \frac{1}{3} \tan x + C$$

$2 \int e^x dx - \frac{1}{3} \int \frac{1}{\cos^3 x} dx$

$x \in (-\frac{\pi}{2}, \frac{\pi}{2}) + 2\pi$   
 $C \in \mathbb{R}$

$$\int \cos(x + \pi) dx \stackrel{C}{=} \sin(x + \pi) \checkmark$$

$\stackrel{?}{=} (\sin(x + \pi))' = \cos(x + \pi)$

$$\int \cos x dx = \sin x$$

$$\int \cos(2x + \pi) dx \stackrel{C}{=} \frac{\sin(2x + \pi)}{2}$$

$(\frac{1}{2} \sin(2x + \pi))' = \frac{1}{2} \cos(2x + \pi) \cdot 2 = \cos(2x + \pi)$

$\rightarrow \frac{1}{2} \sin(2x + \pi) = \frac{2 \cos(2x + \pi)}{2}$

$ax + b$

$2x + \pi$   
 $-x$   
 $\frac{1}{2}x - \frac{\pi}{2}$  ✓

~~$x^2$   
 $\frac{1}{x}$   
 $\sqrt{x}$~~

$$\int \frac{1}{1+x^2} dx \stackrel{C}{=} \arctan x$$

$$\int \frac{1}{1+(4x)^2} dx \stackrel{C}{=} \frac{1}{4} \arctan(4x) \checkmark$$

$$\int \frac{1}{1+16x^2} dx = \frac{1}{4} \arctan(4x)$$