

Topics for Primary seminar, 2021-22

1. Welch two-sample t-test and beyond

Explaining the standard (exact as well as asymptotic) two-sample t-test – the model, the null and the alternative hypothesis, construction of the test statistic.

Introducing the Welch version of the t-test

A detailed explanation of the choice of the degrees of freedom.

Illustrating on the real data set, implementation in R software.

Generalization to more than two samples.

Literature:

Anděl J.: Statistické metody, Matfyzpress, Praha, 1998.

Poznámky k přednášce NMSA331,

<http://msekce.karlin.mff.cuni.cz/~omelka/Soubory/nmsa331/ms1.pdf>

Kurková M (2006). Dvouvýběrový t-test v případě nestejných rozptylů. Bachelor thesis. Faculty of mathematics and physics. Charles University.

Miller Jr, R. G. (1997). Beyond ANOVA: basics of applied statistics. Chapman and Hall/CRC. Chapter 2.3

Satterthwaite F. E.: An Approximate Distribution of Estimates of Variance Components, Biometrics Bulletin 2 (1946), 110–114.

Welch B. L.: The Significance of the Difference Between Two Means when the Population Variances are Unequal, Biometrika 29 (1938), 350– 362.

2. Two sample Wilcoxon test and beyond

Explaining the standard two sample Wilcoxon test – the model, the null and the alternative hypothesis, construction of the test statistic.

Mann-Whitney rank test

Generalizing Mann-Whitney rank test to more general hypothesis

Illustrating what happens if under the alternative hypothesis the distribution does not change only in location.

Dealing with ties

Literature:

Chung, E., & Romano, J. P. (2016). Asymptotically valid and exact permutation tests based on two-sample U-statistics. Journal of Statistical Planning and Inference, 168, 97-105.

Šlampiak, T. (2016). Wilcoxonův dvouvýběrový test. Bachelor thesis. Faculty of mathematics and physics. Charles University.

3. Q-Q plots

Normal Q-Q plot – construction, implementation in R, examples of normal distributions as well distributions that are not normal. Comparison with histogram. Use in linear regression.

General Q-Q plots

Q-Q plots to compare two samples

Literature:

Zvára: Regrese, kapitola 8.7, MATFYZPRESS, 2008 (in Czech),

Wilk, M.B., Gnanadesikan, R. (1968), "Probability plotting methods for the analysis of data", Biometrika, 55 (1): 1–17

4. Permutation tests

Two sample permutation tests (comparision with t-test and Wilcoxon test)

K-sample permutation tests (comparision with ANOVA and Kruskall-Wallis test)

Test of independence

Literature:

Course notes for NMST434, Chapter 8.6, Available at

http://msekce.karlin.mff.cuni.cz/~omelka/Soubory/nmst434/nmst434_course-notes.pdf

Davison, A. C. and Hinkley, D. V. (1997). Bootstrap Methods and their Application. Cambridge University Press, New York. Chapter 4.3.

Efron, B. and Tibshirani, R. J. (1993). An Introduction to the Bootstrap. Chapman & Hall. Chapter 15.

5. Confidence interval, predictive interval and tolerance limits

Introducing and expaling various confidence intervals in the context of a normal distribution

Literature:

Krishnamoorthy, K., Mathew, T.: Statistical tolerance regions. John Wiley, New Jersey, 2009. Chapters 2.2 and 2.3

Otava, M. (2017). Stručný průvodce statistickými intervaly. *Pokroky matematiky, fyziky a astronomie*, 62(1), 7-16. <https://dml.cz/handle/10338.dmlcz/146719>

6. Fisher's exact test and Barnard's test

Explanation of the test, calculation of the p-values (possible different approaches)

Implementation in R software (explaining the R-output).

Comparison with the chi-square test of independence

Illustration on interesting examples

Literature:

Agresti, A.: Categorical data analysis, Second Edition, Wiley, 2002, Chapter 3.5

Anděl, J.: *Statistické metody*. Matfyzpress, Praha, 1998.

Anděl, J.: *Základy matematické statistiky*. Matfyzpress, Praha, 2002.

Kulich, M.: *NMSA 331, Poznámky k přednášce*,

<http://msekce.karlin.mff.cuni.cz/~omelka/Soubory/nmsa331/ms1.pdf>

7. McNemar test, Stuart test, test of symmetry

Explanation of the test, calculation of the p-values

Implementation in R software.

Illustration on interesting examples

Explaining the relationships between the tests

Literature:

Agresti, A.: Categorical data analysis, Second Edition, Wiley, 2002, Chapter 10.1, 10.3

Anděl, J.: *Statistické metody*. Matfyzpress, Praha, 1998.

Anděl, J.: *Základy matematické statistiky*. Matfyzpress, Praha, 2002.

Prášková, Z.: *Kontingenční tabulky*. Univerzita Karlova. Skripta MFF UK, 1985.

8. Some tests for random blocks

Friedman test, Anderson-Kannemann test
Explanation of the test, calculation of the p-values
Implementation in R software.
Illustration on interesting examples
Comparison of the tests

Literature:

- Anděl, J.: *Statistické metody*. Matfyzpress, Praha, 1998.
Anděl, J.: *Základy matematické statistiky*. Matfyzpress, Praha, 2002.
Anderson, R. L. (1959). Use of contingency tables in the analysis of consumer preference studies. *Biometrics*, 15(4), 582-590.
Friedman, M. (1937). The use of ranks to avoid the assumption of normality implicit in the analysis of variance. *Journal of the American Statistical Association*, 32 (200): 675–701.
Friedman, M. (1939). A correction: The use of ranks to avoid the assumption of normality implicit in the analysis of variance. *Journal of the American Statistical Association*. 34 (205): 109.
Kloke, J., and McKean, J. W. (2014). *Nonparametric statistical methods using R*. CRC Press. Chapter 8.2

9. Copulas - introduction.

Sklar's Theorem and its use
Basic properties
Association based on copulas - Spearman's correlation coefficient, Kendall correlation coefficient

Literature: Nelsen, R. B.: An Introduction to Copulas, Second Edition, Springer, 2007, Chapters 2 and 5;
Embrechts, P., Frey, R., & McNeil, A. (2005). Quantitative risk management. Princeton Series in Finance, Princeton, 10. Chapter 5.2

10. Quantile regression

Characterization of quantiles
Regression quantiles with special attention to median regression (LAD)
Using quantiles to illustrate heteroscedasticity
Comparison with the least squares method

Literature:

- Course notes for NMST434, Chapter 5, Available at http://msekce.karlin.mff.cuni.cz/~omelka/Soubory/nmst434/nmst434_course-notes.pdf
Koenker, R. (2005). Quantile Regression. Cambridge University Press, New York.