

Investigate the behavior of the system

$$x' = x(2 - x - y) \tag{1}$$

$$y' = y(x - 1) \tag{2}$$

in the plane  $(t, x) \in \mathbb{R}^2$ . In particular:

**i)** Identify the curves  $x' = 0$ ,  $y' = 0$  and the areas where  $x' > 0$ ,  $x' < 0$ ,  $y' > 0$  and  $y' < 0$ , respectively.

**ii)** Find (all) the equilibrium points.

**ii)** Sketch the dynamics (let the picture be at least 10x10 cm). In particular, outline the dynamics on the coordinate axes ( $x = 0$  or  $y = 0$ ).