

1. Consider the motion of an inviscid homogeneous incompressible fluid ($\mathbb{T} = -p\mathbb{I}$) moving in the absence of body forces. Show that

$$\frac{d}{dt} \int_{\gamma(t)} \mathbf{v} \cdot d\mathbf{x} = 0,$$

where \mathbf{v} denotes the Eulerian velocity field and $\gamma(t)$ is an arbitrary closed curve moving with the fluid, that is $\gamma(t) = \boldsymbol{\chi}(\mathbf{\Gamma}(s), t)$, where $\mathbf{\Gamma}(s)$ is a closed curve in the reference configuration.