

# Algebraic Invariants in Knot Theory

## Practicals 13

Filippo Spaggiari

3 January 2023, Prague

**Exercise 1 (7.1.1, 7.1.6 rev).** Find and prove a formula that determines the number of components of the torus link  $K(q, r)$ . Moreover, show that each component of the torus link  $K(q, r)$  is a torus knot, and determine its parameters.

**Exercise 2.** Let  $q, r \in \mathbb{Z}$  with  $r \neq 0$  and  $\gcd(q, r) = 1$ .

- (i) Show that if  $q = 0, \pm 1$  or  $r = \pm 1$ , then  $K(q, r)$  is the trivial knot.
- (ii) Show that if  $q$  and  $r$  are not equal to 0 and  $\pm 1$  then
  - (a)  $K(-q, r)$  is the mirror image of  $K(q, r)$ .
  - (b)  $K(-q, -r)$  is the knot with opposite orientation of  $K(q, r)$ .
  - (c)  $K(-q, -r)$  is equivalent to  $K(q, r)$ .
  - (d)  $K(q, r)$  is an invertible knot.

**Exercise 3.** Prove that  $K(q, r) \cong K(r, q)$  for every  $q, r \in \mathbb{Z}$ .