

# Mathematics of Life Insurance 1 - Sample test

Max: 20 points      Necessary: 14 points

## Part 1 (3 points)

A loan of 1000 at a nominal rate of 12% convertible monthly is to be repaid by six monthly payments with the first payment due at the end of the first month. The first three payments are  $x$  each, and the final three payments are  $3x$  each. Calculate  $x$ .

## Part 2 (3 points)

Given  $\mu_{x+t} = \frac{1}{85-t} + \frac{3}{105-t}$  for  $0 \leq t < 85$ , calculate  ${}_{20}p_x$ .

## Part 3 (3 points)

Formulate the net single premium of the  $m$ -years deferred endowment with duration  $n$  years  ${}_m|A_{x:\overline{n}|}$  as the expected value of  $Z$  in the sum form. Begin with formulating  $Z$ .

## Part 4 (3 points)

What is the relation between  $\ddot{a}_x$  and  $A_x$ ? Derive it.

## Part 5 (3 points)

Formulate the net single premium of the standard increasing temporary life annuity in advance with duration  $n$  years  $(I\ddot{a})_{x:\overline{n}|}$  as the expected value of  $Y$  in the sum form. Begin with formulating  $Y$ .

## Part 6 (5 points)

Consider  $m$ -years deferred term insurance for  $n$  years, where the annual net premium is paid  $m$  years. Moreover, for the first  $m'$  years (where  $m' < m$ ) during the deferment period the premium refund agreement is active. In the case of death of the insured person 80% of the premium paid until the death is paid to a beneficiary at the end of the year of death. Derive the total loss, the annual net premium and the net premium reserve.